

Algebra II
Lesson 4: Function Notation
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You have already been using function notation and it has shown up in previous lessons. Function notation is the most accurate way to represent a function. The basic form is $f(x)$, the stuff inside parentheses is called the argument of the function. Recognize that x is the **input**. Whatever x is completely determines the output; hence, a functional relationship in terms of x (for this example). When we see an equation written in function form we know that the relationship is a function.

What makes a function?

each element x is related to exactly 1 y ; independent variable
has no repeaters. Passes vertical line test.
Solve for y , if $y =$ only one outcome then function

Example 1... Are the following relations functions? Why or why not?

a. $\{(0,4), (-2,3), (-1,3), (-2,2), (1,-3)\}$

NO
 repeater x

b. $y = x^2 + 5$

Quad
 $y = 1$ outcome
 Yes

c. $3xy + x^2 = 6$

$3xy = -x^2 + 6$
 $y = \frac{-x^2 + 6}{3x}$
 2 y 's for each x
 NO

Instead of just using " $y =$ " function notation uses any letter of the alphabet, and specifies what's going to be the variable in the equation. Write some examples below.

so $y = \frac{x^2 - 7x + 3}{(2x+1)(x-5)}$ function? but! $f(x) = \frac{x^2 - 7x + 3}{(2x+1)(x-5)}$
 don't know

When you see function notation with a number in the parentheses, the number is the value of the independent variable or your input. When you evaluate $f(x)$ for some x , the answer is the dependent variable or output. In other words, substitute the number for every independent variable.

Example 2... Given the functions $f(x) = |x + 1|$ and $h(t) = t^2 + 2t - 1$, evaluate the following.

Sub

a. $f(2)$ Sub 2 in for every x

$f(2) = |2+1| = |3| = 3$

b. $h(3)$

$h(3) = 3^2 + 2(3) - 1$
 $= 9 + 6 - 1$
 $= 14$

c. $h(-1) + f(8)$

$= 1^2 + (2)(-1) + |8+1|$
 $= 1 - 2 + 9$
 $= 8$

d. $2f(-5) - 3h(1)$

Do 1st
 $2(|-5+1|) - 3(1^2 + 2(1) - 1)$
 $2|-4| - 3(2) = 2(4) - 6 = 8 - 6 = 2$

e. $f(c+1)$

$f(c+1) = |c+1+1| = |c+2|$

Solve inside of AbsVal
 1st

Now, let's try evaluation from a table or a graph.

Example 2... Given each table or graph, state the domain and range, determine if the relation is a function and whether it is continuous or discrete. Then evaluate it for $f(-2)$, $f(0)$, and $f(3)$.

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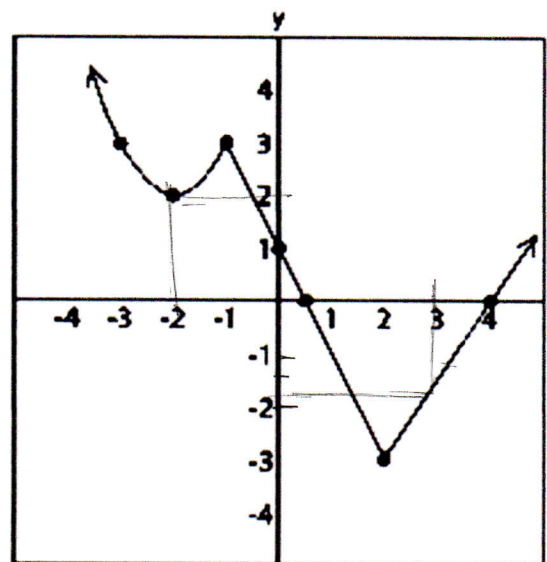
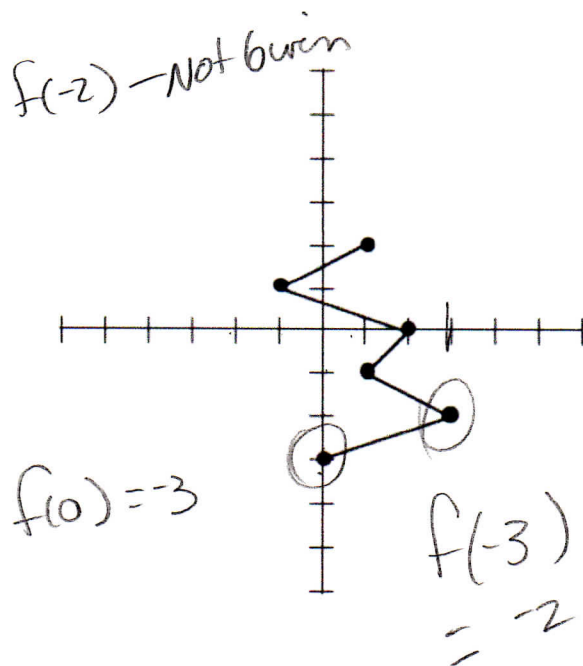
x	$f(x)$
-2	13
-1	12
0	11
1	10
2	9

$f(-2) = 13$
 $f(0) = 11$
 $f(3) = \text{not given}$

→

x	$f(x)$
-3	4
-2	7
1	4
2	-1
3	-8

$f(-2) = 7$
 $f(0) = -8$



$f(0) = 1$
 $f(-2) = 2$
 $f(3) \approx 1.75$